Mass estimates of long-period comets coming close to the Sun

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Abstract

We have estimated the masses of a set of Long-Period Comets (LPCs) (orbital periods $P > 10^3$ yr) with perihelion distances $q < 1.3$ AU and computed nongravitational parameters. We find masses in the range $[0.5 \times 10^3, 12]$ kg, which correspond to diameters $D$ in the range $[1.4, 3.6]$ km for an assumed bulk density of $0.4$ g cm$^{-3}$. Even though large error bars may be attached to these estimates, for the time being we consider this as the first attempt to derive masses of a sample of LPCs in a consistent way. We have next studied the relationship between diameters and absolute total visual magnitudes $H$, and shown that it can be expressed by the lineal relation $\log_{10} D(km) = 1.2 - 0.13H$. In physical terms, this relation implies that the total comet brightness (nucleus + coma) goes as $D^3$. We finally discuss our results in broader terms, as regards the comet size distribution, and the minimum mass or size of an active comet.

The method

Our method follows a procedure similar to that developed by Szutowicz and colleagues ([5], [6]) based on the computed nongravitational parameters, $A_1$, $A_2$, from best-fit orbit solutions, instead of the change in the orbital period $\Delta P$, as done before for a sample of periodic comets (3).

Let $\vec{J}$ be the nongravitational acceleration acting on a comet of mass $M_N$. If $Q$ is the gas production rate, $m$ the mass of the dominant sublimating molecule (H$_2$O in our case), and $v$ the effective outflow velocity, we have (considering modulus):

$$M_N = \frac{Q m v}{J}$$  \hspace{1cm} (1)

where $J = \sqrt{A_1^2 + A_2^2 + A_3^2} \times g(r)$ (it is usually assumed $A_3 = 0$). The function $g(r)$ describes the variation of the sublimation rate of water snow with the heliocentric distance $r$ as adopted by [2].

The water production rate $Q$ has been only determined for a few comets at a few points of their orbits. In order to have a better coverage of different comets, as well as different points along their orbits, we have determined a correlation between the observed $Q$ values and the heliocentric total visual magnitudes $m_h$ (see [4] for more details). Therefore, from the comet’s lightcurve we can derive the water production rate $Q(r)$ at any point of its orbit $r$, in which the sublimation of water snow is significant ($r \lesssim 2.5$ AU), and by means of eq.(1) we can compute $M_N(r)$. For each comet of our sample, we can compute the mean and the standard deviation of the 100 determinations along the orbit. From the computed $< M_N >$, and by assuming a mean bulk density of $0.4$ g cm$^{-3}$, we can derive the mean radius $< R >$ of the comet. We note that the standard deviation shown in Table 1 only considers the dispersion of the 100 computed $M_N$ values along the comet’s orbit, and not other factors of uncertainty as, for instance, in the assumed values of the physical parameters.

Results

Table 1: Estimated mean radii and absolute total visual magnitudes

<table>
<thead>
<tr>
<th>Comet</th>
<th>$&lt; R &gt;$ (km)</th>
<th>$H$</th>
</tr>
</thead>
<tbody>
<tr>
<td>C/1985 R1</td>
<td>0.88 ± 0.05</td>
<td>8.3</td>
</tr>
<tr>
<td>C/1989 Q1</td>
<td>1.00 ± 0.12</td>
<td>7.5</td>
</tr>
<tr>
<td>C/1993 Y1</td>
<td>0.75 ± 0.02</td>
<td>8.7</td>
</tr>
<tr>
<td>C/1995 Y1</td>
<td>1.14 ± 0.02</td>
<td>7.3</td>
</tr>
<tr>
<td>C/1999 J3</td>
<td>0.71 ± 0.01</td>
<td>8.4</td>
</tr>
<tr>
<td>C/2002 V1</td>
<td>1.57 ± 0.16</td>
<td>6.1</td>
</tr>
<tr>
<td>C/2004 Q2</td>
<td>1.82 ± 0.17</td>
<td>5.2</td>
</tr>
<tr>
<td>C/2007 F1</td>
<td>0.75 ± 0.10</td>
<td>8.0</td>
</tr>
<tr>
<td>C/2007 W1</td>
<td>0.65 ± 0.03</td>
<td>8.5</td>
</tr>
</tbody>
</table>

The computed diameters are found to be well correlated to $H$ through the linear relation
\log_{10} D(\text{km}) = 1.2 - 0.13H \quad (2)

By assuming that most of the comet brightness \( B \) was due to sunlight scattered by the dust particles in the coma, [1] found that it is related to the comet’s diameter \( D \) through the relation

\[ B \propto D^3 \quad (3) \]

when the limit of the coma is set by its fading into the sky background. By taking logarithms in eq.(3) and applying the definition of magnitude we arrive at an expression similar to our empirical derivation given by eq.(2).

From the lightcurves of LPCs, we were also able to compute the absolute total visual magnitudes, not only for the comets of Table 1, but for most of the LPCs with \( q < 1.3 \) AU observed during the period 1970-2009. Most of the visual magnitudes were kindly provided by Daniel W. Green (see presentation by Sosa & Fernández for more details). We find that very few comets are fainter than absolute magnitude \( H \sim 13 \), which will correspond to a diameter \( D \sim 0.32 \text{ km} \) according to eq.(2). Our results confirm previous works (e.g. [7]) suggesting that a minimum size is required to have an active comet in the inner planetary region.

From the cumulative distribution of \( H \) found for our sample of LPCs, we can derive the cumulative distribution of comet diameters leading to a bimodal power law:

\[ N(D) \propto D^{-s}, \quad (4) \]

where \( s \simeq 3.7 \) for \( 2.6 \lesssim D \lesssim 5.4 \) km, and \( s \simeq 1.5 \) for \( 1.2 \lesssim D \lesssim 2.6 \) km.

Very bright LPCs approaching or crossing Earth’s orbit with negative values of \( H \) seem to be rare, at least over the studied period of 40 yr. Only one very bright comet appeared: C/1995 O1 (Hale-Bopp) with an estimated \( H = -1.7 \). By applying eq.(2) this corresponds to a diameter \( D = 26 \text{ km} \) which is slightly below some previous estimates (e.g. [8]), but still a sizable comet.

References

We have estimated the masses of a set of Long-Period Comets (LPCs) (orbital periods $P > 10^3$ yr) with perihelion distances $q < 1.3$ AU. However, a few JF comets observed very far from the Sun (4-7 AU) show a wide dispersion of their derived absolute nuclear magnitudes, which suggests that either these JF comets keep active all along the orbit, so the reported unusually bright distant magnitudes were strongly contaminated by a coma, or some of the measured “nuclear magnitudes” were grossly overestimated (i.e., their brightness underestimated). Long-period comets that WISE observed probably got kicked out of the Oort Cloud millions of years ago. The observations were carried out in 2010 during the spacecraft’s primary mission, before it was renamed NEOWISE and reactivated to target near-Earth objects (NEOs) in 2013.

Astronomers already had broader estimates of how many long-period and Jupiter family comets are in our solar system, but had no good way of measuring the sizes of long-period comets. This is because the cloud of gas and dust that surrounds each comet “known as a coma” appears hazy in images and obscures the comet’s nucleus. The results reinforce the idea that comets that pass by the sun more frequently tend to be smaller than those spending much more time away from the sun. Long Period Comets. Seeing comets is an awesome experience. Being able to see a very rare comet in one’s lifetime is truly one unforgettable moment. Comets despite its very bright and seemingly burning appearance are actually bodies of ice in the Solar System. This particular kind of comet is also bound to the Sun by means of gravity. The succeeding orbit of a long period comet can be computed using the comet’s osculating orbit at every epoch after the comet has left the planetary region and the calculations are made with respect to the center of mass of the Solar System. One of the known long period comets is the Comet McNaught.

Some Beliefs About Comets. Comments - No Responses to “Long Period Comets”. Sorry but comments are closed at this time. Being close to the sun is the kiss of death for a comet, and since the orbital period depends only on the average distance from the sun, those that have gotten captured in close do not last long. Halley’s comet makes repeat visits only because it spends most of its time out by Neptune.

There are short term comets and long term comets. The famous Halley’s comet has a period of about 76 years. There have been comets with periods in the thousands of years. The larger the semi-major axis, the larger the period. The orbit of Halley’s Comet â€” from John Walker’s Home Planet Orrery â€” Halley’s comet is the thing in the lower right. Depends on its mass and speed, and if it’s speed based on its mass is sufficient enough to escape the sun’s orbit.